MODELING FOR COMPONENT RELATIONS IN ROBOTIC DISASSEMBLY

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ABSTRACT
Robotic disassembly is a critical technology to achieve automatic disassembly in remanufacturing. However, industrial robots cannot recognize component relations of specific products with various unpredictable states. Therefore, a model for component relations is of great necessity for disassembly optimization problems like Disassembly Sequence Planning (DSP) and Disassembly Line Balancing Problems (DLBP). This paper first introduces the most commonly used models of component relations in three categories. The characteristics of different models are analyzed and compared from the aspects of transformational relations and applications. Finally, suggestions are given as a reference for choosing a suitable component relation model.

Keywords: modeling of component relations, robotic disassembly, disassembly sequence planning, disassembly line balancing

1. INTRODUCTION
Remanufacturing refers to the process of rebuilding end-of-life (EoL) products to their original quality standard (Ilgin and Gupta 2016). It has gained great attention due to both the economic and ecological benefits it creates (Guide Jr 2000). Product disassembly is regarded as the core step of remanufacturing (Tang, et al 2004). However, traditional disassembly process relies on many human workers, which results in great labor costs.

Research efforts in robotic disassembly have been made to increasingly replace manual disassembly. They can execute batch disassembly of easy products independently. The introduction of robots raises several disassembly optimization problems, such as disassembly sequence planning (DSP) and disassembly line balancing (DLB), which are aimed at achieving high efficiency and low time consumption by robots. The preliminary of optimizing those problems is to obtain the internal structure information of EoL product with various unpredictable states. Nevertheless, merely a CAD model is insufficient for getting these component relations.

In order to model the inner structure of products for robotic disassembly, researchers have presented several models. One of the most natural way to represent the connection information between components of a product is liaison graph (Bourjault 1984). Each node of the graph defines a component, while an edge between two nodes indicates that the two components contact to each other. Then matrix-based model of liaisons called interference matrix was presented by Dini and Santochi (1992). To simplify the matrix, Huang, et al (2002) introduced disassembly matrix, which is the integration of interference matrices in all disassembly directions. Except these matrix-based models, graph-based models are also used in representing component relations, like joint precedence graph (Riggs, et al. 2015), AND/OR graph (De Mello and Sanderson 1990) and connector-based precedence graph (Tseng, et al. 2004). Matrix-based and graph-based models are combined by some researchers to convey more information of products. Zhang and Kuo (1997) designed a component fastener graph accompanied with two matrices, adjacency matrix and fasten matrix. Disassembly Petri net is also a popular hybrid-based model with many variations in models of component relations (Zhou and Venkatesh 1999; Guo, et al. 2015). A lot of models are provided but a new issue arises that there are so many models that researchers are confused of choosing a more appropriate one for their problems.

Therefore, this paper compares the most frequently used models of component relations and provides a reference for researchers. Section 2 is devoted to introducing three categories of product model. A discussion of these models from the perspective of transformation and application comparison is shown in Section 3. Finally, section 4 concludes this paper and summarizes the future works.

2. TYPICAL MODELS OF COMPONENT RELATIONS
To obtain feasible sequences from a more comprehensive model, researchers have proposed several kinds of matrices and graphs as the preliminaries of disassembly planning. These models can be clarified as three categories, i.e., matrix-based model, graph-based model, hybrid-based model, as shown in Table 1.
2.1. Matrix-based Models

Commonly used matrix-based models include interference matrix, disassembly precedence matrix and immediate preceded matrix.

(1) Interference Matrix

Interference matrix expresses the interference relations between two components along one or more principal directions.

Assume a product composed of \( n \) components \( E = \{e_1, e_2, \ldots, e_n\} \), the integrated interference matrix in direction \((X-, X^+, Y-, Y^+)\) is a square matrix of order \( n \) as defined in Eq. (1).

\[
H_{int} = \begin{bmatrix}
h_{11} & h_{12} & h_{13} & \cdots & h_{1n} \\
h_{21} & h_{22} & h_{23} & \cdots & h_{2n} \\
h_{31} & h_{32} & h_{33} & \cdots & h_{3n} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
h_{n1} & h_{n2} & h_{n3} & \cdots & h_{nn}
\end{bmatrix}
\]

In addition, interference matrix is usually used together with many complementary matrices such as contact matrix and connection matrix proposed by Dini and Santochi (1992).

(2) Disassembly Precedence Matrix

There are two types of disassembly precedence matrix (DPM) to show the precedence relations, static DPM and dynamic DPM. Static DPM and its variations mentioned in later references (Tseng, et al. 2011; González and Adenso-Díaz, 2006) somehow has more similarities to interference matrix.

As the precedence relations vary during the disassembly process, dynamic DPM is established by Tao, et al (2018) to reflect these changes.

Dynamic DPM consists of four sub-matrices, a connection matrix between components and fasteners (CFM), a motion constraint matrix for fasteners (FCM), a motion constraint matrix for components (CCM), and a precedence matrix between fasteners (FFM). Element in these matrices represents the disassembly precedence between fasteners and components.

The variable \( h_{ij} = 1 \) means that \( e_i \) impedes \( e_j \) in direction \( k \), otherwise \( h_{ij} = 0 \). As no component interferes with itself, \( h_{mm} = 0 \), \( m \in [1,n] \) equals 0. The interference matrix can be automatically extracted from CAD model of the product (Zhang, et al. 2017).

Huang, et al. (2002) proposed to use the Boolean OR operator to check each component that if there exists one direction in which no precedent component hinders its removal. An example product and its interference matrix are given in Figure 1.

(3) Immediate Preceded Matrix

Immediate preceded matrix (IPM) is also termed as immediately preceding matrix (Kalayci and Polat 2014). Each element in an IPM defines a disassembly operation/task instead of a component/fastener. Therefore, the task precedence relations are shown by IPM(\( y_{ij} \), \( y_{ij} \) is equal to 1 if task \( i \) should be executed after task \( j \), otherwise it is 0.

Using IPM alone is not enough for disassembly line balancing. It is usually accompanied with an assignment
matrix $[x_{ij}]_{m \times n}$ to state the partition of total tasks, where $m$ denotes the number of workstations (Kalayci and Polat 2014; Kalayci and Gupta 2013). If part $j$ is assigned to station $k$, corresponding element $x_{jk}$ equals to 1, otherwise it is 0.

$$t_i = \sum_{q \in Q} p_q t_{iq} \quad \forall i \in I$$  

There are in total of $Q$ models. $t_{iq}$ represents the processing time of the $i^{th}$ task. $p_q$ is defined as a demand portion to represent the weight of the $q^{th}$ model. These weights satisfy $\sum_{q \in Q} p_q = 1$. Therefore, $t_i$ is the resultant average processing time of node $i$. The nodes of the resultant graph are the union set of the sub-graphs correspond to different models. An example JPG is shown in Figure 2. The arcs of the resultant graph are obtained by Eq. (3). Redundant arcs are defined as the ones that not exist in the critical path of a process.

$$E=\bigcup_{q \in Q} E_q \setminus \{\text{redundant arcs}\}$$

(3) AND/OR Graph

AND/OR graph (AOG) is introduced by De Mello and Sanderson (1990) to connect disassembly task, components and subassemblies. Nodes in AOG indicate possible subassemblies and components. Parent and children subassemblies are connected by a pair of directed arcs representing disassembly tasks. The arcs are AND-type. If there are multiple optional operations for a parent node, OR-type relation is used between different pairs of AND-type-arcs to show possible disassembly processes. A disassembly sequence will be generated by choosing OR-type-arcs with connected sub-graphs.

AOG enumerates all possible operations for disassembling a product. One can traverse the graph to find the optimal disassembly sequence (Ghandi and Masehian 2015), but it is not practical. In order to avoid excessively complex graph search, Lambert (1999) proposed to use hyper-arcs to avoid repeated nodes and
simplify the graph. An improved AOG of the sample product of Figure 1(a) is given in Figure 3.

(4) Transformed AND/OR Graph

Transformed AND/OR graph (TAOG) is introduced by Koc, et al. (2009). It is a clearer and more efficient model than AOG.

There are two types of nodes in a TAOG, i.e., artificial node and normal node. Artificial node \( A_i \) defines subassembly or component to be disassembled, while normal node \( B_i \) represents possible disassembly operation. Therefore, the two kinds of nodes are connected alternately. A group of OR-type arcs points from an artificial node to normal nodes defines optional operations. Only one of these operations can be executed at one time. A set of AND-type arcs that start from a normal node and end at several artificial nodes indicates the resultant parts by the specific operation.

With the precedence relations still satisfied and nodes connected by the two kinds of arcs, a TAOG can be formed or transformed from an AOG.

(5) Connector-based Precedence Graph

Connector-based precedence graph (CPG) is originally proposed to deal with assembly sequence planning by Tseng, et al. (2004). Considering the definition of connectors provided in the paper, a product can be decomposed into a set of connector-based elements, thus the graph is also applicable in disassembly problems. A node in CPG refers to a connector or fastener, with its assembly/disassembly information, such as disassembly directions, tools, and precedence constraints. In assembly problems, CPG has a start point representing the state that all connectors are not assembled yet and a terminal point representing full product. Directed arc between two nodes shows their precedence relations.

(6) Disassembly Constraint Graph

Disassembly constraint graph (DCG) introduced by Li, et al. (2005) minimizes model complexity and simplifies the process of generating disassembly sequences for selective disassembly. A DCG is defined as a triple \( M = \{ V, E, D E \} \). \( V \) is a node set containing components and subassemblies which cannot be dismantled further. \( E \) is an undirected edge set containing disassembly contact constraints between components and also represent the disassembly operations. \( DE \) is a directed edge set describing precedence information between components. Li, et al. (2005) have developed a method to identify non-contact adjacent nodes and subassemblies in a DCG within a short time.

2.3. Hybrid-based Model

By hybridizing matrix and graphs, models like component-fastener graph, disassembly hybrid graph model and disassembly Petri net, can extract more information from CAD model.

(1) Component-fastener Graph

Component-fastener graph, denoted as \( G_c = (V, E) \), is presented by Zhang and Kuo (1997).

It can be retrieved from a CAD model providing required information, like the name of components, disassembly method and connection relationship between components. The \( n \) components are labeled as \( \{v_1, v_2, \cdots, v_n\} \) in the vertex set \( V \). The relations between these vertices are indicated as a set of undirected edges \( E = \{e_1, e_2, \cdots, e_n\} \). All the component and fastener information in need is included in the vertex, such as its name, weight and material type.

Elements in two auxiliary matrix, adjacency matrix \( E_c \) and fasten matrix \( F_c \) are defined respectively in Eq. (4) and Eq. (5).

\[
E_{c,ij} = \begin{cases} 
1, & \text{if the component } i \text{ is connected with component } j \\
0, & \text{otherwise}
\end{cases} \quad (4)
\]

\[
F_{c,ij} = \begin{cases} 
1, & \text{if the component } i \text{ is connected with component } j \text{ by } k \text{ fasteners} (k > 0) \\
0, & \text{otherwise}
\end{cases} \quad (5)
\]

(2) Disassembly Hybrid Graph Model

Disassembly hybrid graph model (DHGM) is proposed by Zhang, et al (2010) to record both mating contact and noncontact precedence relationships among components. A DHGM is denoted as \( G = \{V, E_f, E_c, E_{pc}\} \), where node set \( V \) contains the minimal disassembly units (components or subassemblies). \( E_f \) contains undirected edges that denotes contact constraints. \( E_{pc} \) is a directed solid edge set in which the edges represent both contact constraints and precedence relations. Directed dotted edges in \( E_f \) define the priority relationships between two units. A DHGM of sample product in Figure 1(a) is shown in Figure 4.
(3) Disassembly Petri Net

Disassembly Petri net (DPN) varies in different definitions. In this paper, an 8-tuple Petri net presented by Guo, et al. (2015) is introduced. DPN can be defined as $DPN = (S, T, I, O, M, c, r, w)$, where $S$ is a place set containing $n$ disassembly parts (the number of components or subassemblies). $T$ records a set of transitions representing disassembly operations. $I$ is an input function that defines a set of directed arcs from $T$ to $S$. $O$ is an output function defining arcs from $S$ to $T$. $M = \{M_1, \ldots, M_n\}$ is a mark set. Each element $M_i$ represents the number of tokens in place $S_i$, $i = 1, 2, \ldots, n$. $c$ is disassembly cost associated with each disassembly operation. $r$ is corresponding recycling/reuse value of each place. $w$ is a set of weight functions corresponding to the transitions. A DPN of sample product in Figure 2(a) is shown in Figure 5.

![Figure 4: DHGM of Sample Product in Figure 2(a)](image)

Two matrices, precedence matrix $U = [u_{ij}]$ and disassembly matrix $D = [d_{ij}]$, are also adopted (Guo, et al. 2015) and specified in Eq. (6) and (7).

$$u_{ij} = \begin{cases} 
1, & \text{if operation } t_i \text{ need to be performed after } t_j \noindent \text{ performed after } t_j \\
0, & \text{otherwise} 
\end{cases} \quad (6)$$

$$d_{ij} = \begin{cases} 
1, & \text{if disassembly unit } s_j \text{ is obtained via operation } t_i \\
-1, & \text{if } s_j \text{ is disassembled via } t_i \\
0, & \text{otherwise} \end{cases} \quad (7)$$

3. TRANSFORMATION AND COMPARISON BETWEEN DIFFERENT MODELS

Twelve frequently used models of component relations are already introduced hereinafter, although it is possible that there are still some remarkable ones not mentioned. Although those models vary, all of them are able to provide essential information for solving disassembly optimization problems such as DLP and DLBP. This section aims at offering a reference for those confused of choosing the model better for their problems.

A comparison between the models is given in Table 3 and the transformational relations are also included. As shown in the table, it is noticeable that three categories of models can be converted to each other in some ways. However, differences still exist between those models. By contrast, matrix-based models like IM, DPM is easier to extract from others, while hybrid ones like DHGM, DPN are more informative therefore difficult to obtain. Almost all models based on components can be derived from a CAD model. Without definitions of each task and other necessary information, a component-based model cannot be transformed directly to a task-based one. Apart from those based on either components or tasks, models based on both of them, such as AOG and TAOG, are commonly applied to solve disassembly problems as well. The two models can be converted to each other. To replace repeated and long-hour manual work, some automatic generating methods are presented. Zhang, et al. (2016) proposed an algorithm to generate improved IMs.

![Figure 5: Disassembly Petri Net of the Sample Product Shown in Figure 1(a)](image)
Table 2: Transformation

<table>
<thead>
<tr>
<th>No.</th>
<th>Category</th>
<th>Name</th>
<th>Task-based model or component-based</th>
<th>Transformable from CAD model?</th>
<th>Can be transformed to</th>
<th>Can be generated from</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Matrix</td>
<td>IM</td>
<td>Component-based</td>
<td>YES</td>
<td>DPM</td>
<td>DPM, CPG, DCG, DHGM, DPN</td>
</tr>
<tr>
<td>2</td>
<td></td>
<td>DPM</td>
<td>Component-based</td>
<td>YES</td>
<td>IM</td>
<td>IM, CPG, DCG, DHGM, DPN</td>
</tr>
<tr>
<td>3</td>
<td></td>
<td>IPM</td>
<td>Task-based</td>
<td>NO</td>
<td>TPD</td>
<td>TPD, JPG, AOG, DPN</td>
</tr>
<tr>
<td>4</td>
<td></td>
<td>TPD</td>
<td>Task-based</td>
<td>NO</td>
<td>IPM</td>
<td>IPM, JPG, AOG, DPN</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>JPG</td>
<td>Task-based</td>
<td>NO</td>
<td>IM, TPD</td>
<td>/</td>
</tr>
<tr>
<td>6</td>
<td></td>
<td>AOG</td>
<td>Task-and-component based</td>
<td>YES</td>
<td>TAOG</td>
<td>TAOG, DPN</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td>TAOG</td>
<td>Task-and-component based</td>
<td>YES</td>
<td>AOG</td>
<td>AOG, DPN</td>
</tr>
<tr>
<td>8</td>
<td></td>
<td>CPG</td>
<td>Component-based</td>
<td>YES</td>
<td>IM, DPM, CPG</td>
<td>CFG</td>
</tr>
<tr>
<td>9</td>
<td></td>
<td>DCG</td>
<td>Component-based</td>
<td>YES</td>
<td>IM, DPM</td>
<td>DHGM</td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>CFG</td>
<td>Component-based</td>
<td>YES</td>
<td>CPG</td>
<td>/</td>
</tr>
<tr>
<td>11</td>
<td></td>
<td>DHGM</td>
<td>Component-based</td>
<td>YES</td>
<td>IM, DPM, DCG</td>
<td>/</td>
</tr>
<tr>
<td>12</td>
<td></td>
<td>DPN</td>
<td>Task-and-component based</td>
<td>YES</td>
<td>IM, DPM, IPM, TPD, AOG, TAOG</td>
<td>/</td>
</tr>
</tbody>
</table>

Furthermore, all of the above models are capable of recording disassembly state and assisting with real-time updates, which is not mentioned in the table. Some of them works by modifying the model to eliminate the dismantled part immediately, like IM, dynamic DPM and so on. Some label the current separated progress at the node of component or task, instead of changing the original model of component relations.

Table 3: Applications

<table>
<thead>
<tr>
<th>No.</th>
<th>Category</th>
<th>Name</th>
<th>Space(model) complexity</th>
<th>Disassembly sequence planning</th>
<th>Disassembly line balancing</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Matrix</td>
<td>IM</td>
<td>O(N^2D)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>2</td>
<td></td>
<td>DPM</td>
<td>O(N^2 D)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>3</td>
<td></td>
<td>IPM</td>
<td>O(T')</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>4</td>
<td></td>
<td>TPD</td>
<td>O(T')</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>JPG</td>
<td>O(T')</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>6</td>
<td></td>
<td>AOG</td>
<td>Uncertain</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td>TAOG</td>
<td>O[(2N)^2]</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>8</td>
<td></td>
<td>CPG</td>
<td>O(C^2)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>9</td>
<td></td>
<td>DCG</td>
<td>O(N^2)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>10</td>
<td>Hybrid</td>
<td>CFG</td>
<td>O(N^2)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>11</td>
<td></td>
<td>DHGM</td>
<td>O(N^2)</td>
<td>√</td>
<td>/</td>
</tr>
<tr>
<td>12</td>
<td></td>
<td>DPN</td>
<td>Uncertain</td>
<td>√</td>
<td>/</td>
</tr>
</tbody>
</table>

From the perspective of disassembly completion, there are three types of disassembly, complete disassembly, selective disassembly and partial disassembly. Most researches about modeling for component relations are devoted to completely disassembly. Only a few of them have been applied to solve two incomplete separations, such as IM and DCG. Nevertheless, not all parts of EoL products are valuable and reusable. What really matters for manufacturers is how to collect those components of high recovery value within the least time duration. Therefore, the latter two disassembly problems are supposed to be paid more attention.

4. CONCLUSIONS

Rapid development of remanufacturing brings challenges and opportunities for product manufacturing industry. Compared with those other new fields, there is no doubt that robotic disassembly attracts more attention. Most optimization problems in this field start with
modeling for component relations. Therefore, this paper concludes three typical categories of component relation models, matrix-based model, graph-based model and hybrid-based model. Model comparison from perspectives of transformation and application were also discussed, which provides a reference for choosing more suitable component relation models in robotic disassembly optimization problems.

So far, most of the existing models of component relations are designed for completely disassembly. However, it usually takes plenty of time for robot to dismantle unnecessary parts in this kind of disassembly process. Modeling for selective and partial disassembly would be a fruitful area for future work.

CAD model of an EoL product contains various information of products. Only several models of component relations can be obtained with automatic generating algorithms if CAD models are provided. To make use of other models, manual work is still required, which undoubtably will take a lot of time. Future research can be conducted to reduce human involvement in model generation process.

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